



# Evaluating a model graphically

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## Plotting Ground Truth vs. Predictions



#### A poorly fitting model

Servo response time vs. linear model prediction



- x = y line runs through center of points
- "line of perfect prediction"

- Points are all on one side of x = *y* line
- Systematic errors



### The Residual Plot

#### A well fitting model

Residuals vs. linear model prediction



#### A poorly fitting model

Residuals vs. linear model prediction



- Residual: actual outcome prediction
- Good fit: no systematic errors

• Systematic errors





#### The Gain Curve



Measures how well model sorts the outcome

• **x-axis**: houses in model-sorted

order (decreasing)

• y-axis: fraction of total

accumulated home sales

Wizard curve: perfect model

## Reading the Gain Curve



GainCurvePlot(houseprices, "prediction", "price", "Home price model")





## Let's practice!





## Root Mean Squared Error (RMSE)

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#### What is Root Mean Squared Error (RMSE)?

$$RMSE = \sqrt{(pred - y)^2}$$

where

- pred y: the error, or residuals vector
- $\overline{(pred y)^2}$ : mean value of  $(pred y)^2$



### RMSE of the Home Sales Price Model

# Calculate error > err <- houseprices\$prediction - houseprices\$price</pre>

- price: column of actual sale prices (in thousands)
- prediction: column of predicted sale prices (in thousands)



#### **RMSE** of the Home Sales Price Model

# Calculate error > err <- houseprices\$prediction - houseprices\$price</pre>

# Square the error vector

> err2 <- err^2



#### RMSE of the Home Sales Price Model

```
# Calculate error
> err <- houseprices$prediction - houseprices$price</pre>
# Square the error vector
> err2 <- err^2
# Take the mean, and sqrt it
> (rmse <- sqrt(mean(err2)))</pre>
[1] 58.33908
```

•  $RMSE \approx 58.3$ 



## Is the RMSE Large or Small?

# Take the mean, and sqrt it > (rmse <- sqrt(mean(err2)))</pre> [1] 58.33908

# The standard deviation of the outcome > (sdtemp <- sd(houseprices\$price))</pre> [1] 135.2694

- $RMSE \approx 58.3$
- $sd(price) \approx 135$





## Let's practice!





## **R-Squared** ( $R^2$ )

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### What is $R^2$ ?

A measure of how well the model fits or explains the data

- A value between 0-1
  - near 1: model fits well
  - near 0: no better than guessing the average value



## Calculating $R^2$

 $R^2$  is the variance explained by the model.

$$R^2 = 1 - rac{RSS}{SS_{Tot}}$$

where

- $RSS = \sum (y prediction)^2$ 
  - Residual sum of squares (variance from model)
- $SS_{Tot} = \sum (y \overline{y})^2$ 
  - Total sum of squares (variance of data)



## Calculate $R^2$ of the House Price Model: RSS

- Calculate error
- > err <- houseprices\$prediction houseprices\$price</pre>
  - Square it and take the sum

> rss <- sum(err^2)</pre>

- price: column of actual sale prices (in thousands)
- pred: column of predicted sale prices (in thousands)
- $RSS \approx 136138$



## Calculate $R^2$ of the House Price Model: $SS_{Tot}$

- Take the difference of prices from the mean price
- > toterr <- houseprices\$price mean(houseprices\$price)</pre>
  - Square it and take the sum
- > sstot <- sum(toterr^2)</pre>
  - $RSS \approx 136138$
  - $SS_{Tot} \approx 713615$





## Calculate $R^2$ of the House Price Model

- > (r\_squared <- 1 (rss/sstot) )</pre> [1] 0.8092278
  - $RSS \approx 136138$
  - $SS_{Tot} \approx 713615$
  - $R^2 \approx 0.809$



## Reading $R^2$ from the Model

For Im() models:

• From summary():

```
> summary(hmodel)
## ...
## Residual standard error: 60.66 on 37 degrees of freedom
## Multiple R-squared: 0.8092, Adjusted R-squared: 0.7989
## F-statistic: 78.47 on 2 and 37 DF, p-value: 4.893e-14
> summary(hmodel)$r.squared
```

- [1] 0.8092278
  - From glance():

> glance(hmodel)\$r.squared
[1] 0.8092278

## Correlation and $R^2$

> rho <- cor(houseprices\$prediction, houseprices\$price)</pre> [1] 0.8995709

 $> rho^2$ [1] 0.8092278

•  $\rho = cor(prediction, price) = 0.8995709$ 

• 
$$\rho^2 = 0.8092278 = R^2$$

- True for models that minimize squared error:
  - Linear regression
  - GAM regression
  - Tree-based algorithms that minimize squared error
- True for training data: NOT true for future application data





## Let's practice!





## Properly Training a Model

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## Models can perform much better on training than they do on future data.



• Training  $R^2$ : 0.9; Test  $R^2$ : 0.15 -- **Overfit** 



## Test/Train Split



Recommended method when data is plentiful



#### Example: Model Female Unemployment



• Train on 66 rows, test on 30 rows



#### Model Performance: Train vs. Test



- Training: RMSE 0.71,  $R^2$  0.8
- Test: RMSE 0.93, *R*<sup>2</sup> 0.75





Preferred when data is not large enough to split off a test set















### Create a cross-validation plan

- > library(vtreat)
- > splitPlan <- kWayCrossValidation(nRows, nSplits, NULL, NULL)</pre>
  - nRows: number of rows in the training data
  - nSplits: number folds (partitions) in the cross-validation
    - e.g, nfolds = 3 for 3-way cross-validation
  - remaining 2 arguments not needed here



#### Supervised Learning in R: Regression

### Create a cross-validation plan

```
> library(vtreat)
```

> splitPlan <- kWayCrossValidation(10, 3, NULL, NULL)</pre>

First fold (A and B to train, C to test)

```
> splitPlan[[1]]
## $train
## [1] 1 2 4 5 7 9 10
##
## $app
## [1] 3 6 8
```

Train on A and B, test on C, etc...

```
> split <- splitPlan[[1]]
> model <- lm(fmla, data = df[split$train,])
> df$pred.cv[split$app] <- predict(model, newdata = df[split$app,])</pre>
```



## Final Model





### Example: Unemployment Model

Measure type	RMSE	$R^2$
train	0.7082675	0.8029275
test	0.9349416	0.7451896
cross-validation	0.8175714	0.7635331





## Let's practice!